Deforming pro-p groups

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Abstract

It is a classical result due to Zassenhaus and Jennings, that every prop group G defines a restricted (1-generated) N_0 -graded F_p -Lie algebra $gr_{\bullet}(G)$. For such a restricted F_p -Lie algebra L_{\bullet} , one defines the genus of L_{\bullet} as the set of isomorphisms classes of pro-p groups [G] satisfying $gr_{\bullet}(G) \simeq L_{\bullet}$. Therefore, one may interpret $gen(G) = gen(gr_{\bullet}(G))$ as the set of canonical deformations of the pro-p group G. We will discuss some recent results and open problems concerning the genus.